Prof. Dr. Alfred Toth

Topologische Werte semiotischer Subrelationen

1. In dieser Arbeit werden die bisherigen Ergebnisse der topologischen Semiotik (vgl. zuletzt Toth 2013a, b) dadurch zusammengefaßt, daß die topologischen Werte für Grenzen, Ränder, Grenzränder, Nachbarschaften und Umgebungen aller 9 semiotischen Subrelationen (Subzeichen) gegeben werden, wie sie in der semiotischen Matrix (vgl. Bense 1975, S. 37) erscheinen.

2.1. R = (1.1)

G(1.1, 1.1) = (1.1)

R_λ(1.1) = Ø

R_ρ(1.1) = (1.2, 1.3, 2.1, 3.1)

$\mathfrak{G}_\lambda$ = G(1.1) ∩ Ø = Ø

$\mathfrak{G}_\rho$ = G(1.1) ∩ (1.2, 1.3, 2.1, 3.1) = Ø

N(1.1) = {1.2, 2.1, 2.2}

U(1.1) = {1.3, 2.3, 3.1, 3.2, 3.3}

N(U(1.1)) = {1.2, 2.1, 2.2}.

2.2. R = (1.2)

G(1.2, 2.1) = (1.2, 2.1)

R_λ(1.2) = (1.1)

R_ρ(1.2) = (1.3, 2.2, 3.2)

$\mathfrak{G}_\lambda$ = G(1.2, 2.1) ∩ (1.1) = Ø

$\mathfrak{G}_\rho$ = G(1.2, 2.1) ∩ (1.3, 2.2, 3.2) = Ø

N(1.2) = {1.1, 1.3, 2.1, 2.2, 2.3}

U(1.2) = {3.1, 3.2, 3.3}

N(U(1.2)) = (2.1, 2.2, 2.3).

2.3. R = (1.3)

$R_\lambda(1.3) = (1.1, 1.2)$

$R_\rho(3.1) = (3.2, 3.3)$

$\mathfrak{G}_\lambda = G(1.3, 3.1) \cap (1.1, 1.2) = \emptyset$

$\mathfrak{G}_\rho = G(1.3, 3.1) \cap (2.3, 3.3) = \emptyset$

N(1.3) = {1.2, 2.2, 2.3}

U(1.3) = {1.1, 2.1, 3.1, 3.2, 3.3}

N(U(1.3)) = {1.2, 2.2, 2.3).

2.4. R = (2.1)

G(2.1, 1.2) = (2.1, 1.2)

$R_\lambda(2.1) = (1.1)$

$R_\rho(2.1) = (2.2, 2.3, 3.1)$

$\mathfrak{G}_\lambda = G(2.1, 1.2) \cap (1.1) = \emptyset$

$\mathfrak{G}_\rho = G(2.1, 1.2) \cap (2.2, 2.3, 3.1) = \emptyset$

N(2.1) = {1.1, 1.2, 2.2, 3.1, 3.2}

U(2.1) = {1.3, 2.3, 3.3}

N(U(2.1)) = {1.2, 2.2, 3.2}.

2.5. R = (2.2)

G(2.2, 2.2) = (2.2)

$R_\lambda(2.2) = (1.2, 2.1)$

$R_\rho(2.2) = (2.3, 3.2)$

$\mathfrak{G}_\lambda = G(2.2) \cap (1.2, 2.1) = \emptyset$

$\mathfrak{G}_\rho = G(2.2) \cap (2.3, 3.2) = \emptyset$

N(2.2) = {1.1, 1.2, 1.3, 2.1, 2.3, 3.1, 3.2, 3.3}

U(2.2) = Ø

$N(U(2.2)) = \mathfrak{M}_{3\times3.}$

2.6. R = (2.3)

G(2.3, 3.2) = (2.3, 3.2)

$R_\lambda(2.3) = (1.3, 2.1, 2.2)$

$R_\rho(2.3) = (3.3)$

$\mathfrak{G}_\lambda = G(2.3, 3.2) \cap (1.3, 2.1, 2.2) = \emptyset$

$\mathfrak{G}_\rho = G(2.3, 3.2) \cap (3.3) = \emptyset$

N(2.3) = {1.2, 1.3, 2.2, 3.2, 3.3}

U(2.3) = {1.1, 2.1, 3.1}

N(U(2.3)) = {1.2, 2.2, 3.2}.

2.7. R = (3.1)

G(3.1, 1.3) = (1.3, 3.1)

$R_\lambda(3.1) = (1.1, 2.1)$

$R_\rho(3.1) = (3.2, 3.3)$

$\mathfrak{G}_\lambda = G(3.1, 1.3) \cap (1.1, 2.1) = \emptyset$

$\mathfrak{G}_\rho = G(3.1, 1.3) \cap (3.2, 3.3) = \emptyset$

N(3.1) = {2.1, 2.2, 3.2}

U(3.1) = {1.1, 1.2, 1.3, 2.3, 3.3}

$N(U(3.1)) = \{2.1, 2.2, 3.2\}$.

2.8. $R = (3.2)$

$G(3.2, 2.3) = (2.3, 3.2)$

$R_\lambda(3.2) = (1.2, 2.2, 3.1)$

$R_\rho(3.2) = (3.3)$

$\mathfrak{G}_\lambda = G(3.2, 2.3) \cap (1.2, 2.2, 3.1) = \emptyset$

$\mathfrak{G}_\rho = G(3.2, 2.3) \cap (3.3) = \emptyset$

$N(3.2) = \{2.1, 2.2, 2.3, 3.1, 3.3\}$

$U(3.2) = \{1.1, 1.2, 1.3\}$

$N(U(3.2)) = \{2.1, 2.2, 2.3\}$.

2.9. $R = (3.3)$

$G(3.3, 3.3) = (3.3)$

$R_\lambda(3.3) = (1.3, 2.3, 3.1, 3.2)$

$R_\rho(2.1) = \emptyset$

$\mathfrak{G}_\lambda = G(3.3) \cap (1.3, 2.3, 3.1, 3.2) = \emptyset$

$\mathfrak{G}_\rho = G(3.3) \cap \emptyset = \emptyset$

$N(3.3) = \{2.2, 2.3, 3.2\}$

$U(3.3) = \{1.1, 1.2, 1.3, 2.1, 3.1\}$

$N(U(3.3)) = \{2.2, 2.3, 3.2\}$.

Literatur

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